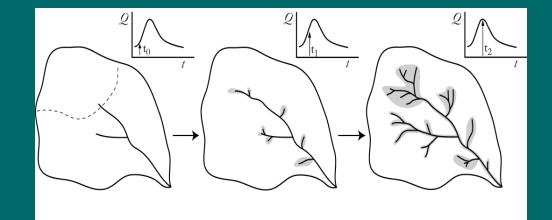
Modélisation numérique des interactions eaux souterraines / eaux de surface: défis et progrès récents



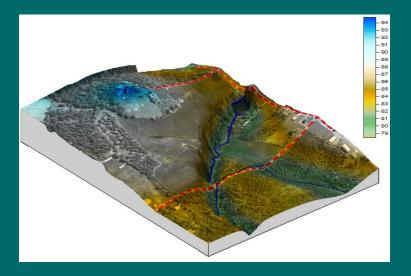
### **Claudio Paniconi**

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82<sup>e</sup> Congrès de l'ACFAS, Concordia University, 13 mai, 2014

## Context

Proper understanding and representation of hydrosphere interactions (between the atmosphere, land surface, soil zone, aquifers, rivers/lakes, and vegetation) is increasingly relevant to climate prediction, environmental protection, and water management



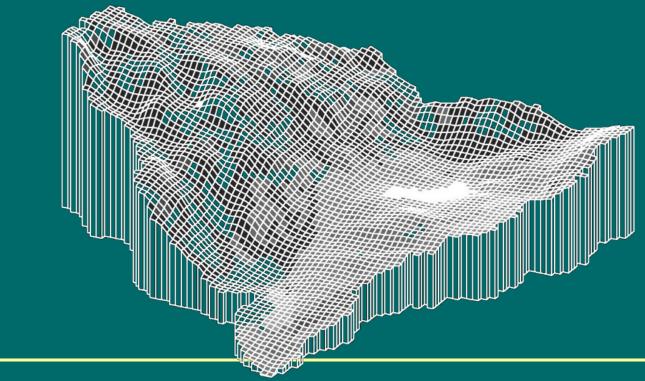
We are at a crossroads in hydrological modeling:

- models (of all flavors) are being integrated across many disciplines and over multiple scales, and they are being intercompared
- better datasets are increasingly being made available (for hypothesis testing and model validation) that provide observations (on the ground, airborne, and from space) of more processes, in more detail, and at higher accuracy
- computational boundaries are continually being pushed (cost and capabilities of systems, efficiency and robustness of algorithms), for easier and more effective data analysis and process simulation

CATHY (CATchment HYdrology) model description

Some recent studies (successes and challenges)

Extensions and evolution of the model



### CATHY (CATchment HYdrology) model description

$$\sigma(S_w) \frac{\partial \psi}{\partial t} = \nabla \cdot \left[ K_s K_{rw}(S_w) (\nabla \psi + \eta_z) \right] + q_s(h)$$

$$\frac{\partial Q}{\partial t} + c_k \frac{\partial Q}{\partial s} = D_h \frac{\partial^2 Q}{\partial s^2} + c_k q_L(h, \psi)$$
<sup>(2)</sup>

 $\sigma$   $S_{w} \theta$   $\theta_{s}$   $S_{s} \phi$   $\psi$  t  $K_{s}$   $K_{rw}$   $\eta_{z}$ 

general storage term [1/L]:  $\sigma = S_w S_s + \phi(dS_w/d\psi)$ water saturation =  $\theta/\theta_s$  [/] volumetric moisture content [L<sup>3</sup>/L<sup>3</sup>] saturated moisture content [L<sup>3</sup>/L<sup>3</sup>] specific storage [1/L] porosity (=  $\theta_s$  if no swelling/shrinking) pressure head [L] time [T] saturated conductivity tensor [L/T] relative hydraulic conductivity [/] zero in *x* and *y* and 1 in *z* direction

2	vertical coordinate +ve upward [L]
$\gamma_{\rm s}$	subsurface equation coupling term
Ŭ	(more generally, source/sink
	term) $[L^3/L^3T]$
า	ponding head (depth of water on
	surface of each cell) [L]
5	hillslope/channel link coordinate [L]
Q	discharge along s [L <sup>3</sup> /T]
$\mathbf{\hat{F}}_{k}$	kinematic wave celerity [L/T]
$\dot{D}_h$	hydraulic diffusivity [L <sup>2</sup> /T]
$\frac{1}{2}$	surface equation coupling term
	(overland flow rate) [L <sup>3</sup> /LT]

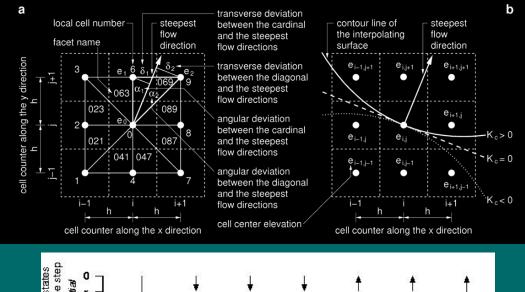
(1) Paniconi & Wood, Water Resour. Res., 29(6), 1993 ; Paniconi & Putti, Water Resour. Res., 30(12), 1994

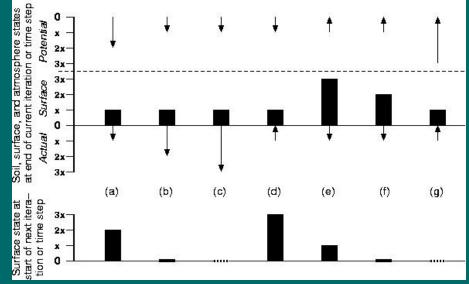
(2) Orlandini & Rosso, J. Hydrologic Engrg., ASCE, 1(3), 1996; Orlandini & Rosso, Water Resour. Res., 34(8), 1998

(1)+(2) Putti & Paniconi, CMWR Proceedings, 2004; Camporese, Paniconi, Putti, & Orlandini, Water Resour. Res., 46(W02512), 2010

Path-based description of surface flow across the drainage basin; several options for identifying flow directions, for separating channel cells from hillslope cells (same governing equation), and for representing stream channel hydraulic geometry.

The coupling term for the model is computed as the balance between atmospheric forcing (rainfall and potential evaporation) and the amount of water that can actually infiltrate or exfiltrate the soil. This threshold-based boundary condition switching partitions potential fluxes into actual fluxes and changes in surface storage.





Various functional forms for  $S_w(\psi)$  and  $K_{rw}(\psi)$ 

Heterogeneities ( $K_{sx}$ ,  $K_{sy}$ ,  $K_{sz}$ ,  $S_s$ ,  $\phi$ ) by "zone" and by layer

DEM-based (uniform) grid or user-defined (nonuniform) surface grid input

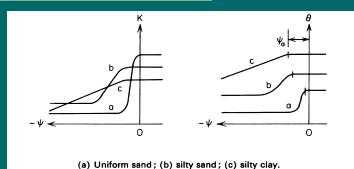
3D grid automatically generated with variable layer thicknesses and different base ("bedrock") shapes

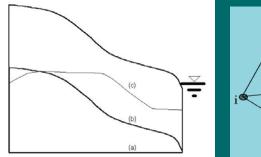
Finite element spatial integrator (Galerkin scheme, tetrahedral elements, linear basis functions)

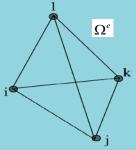
Weighted finite difference discretization in time

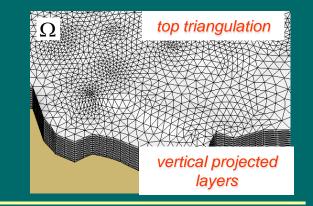
Time-varying boundary conditions: Neumann, Dirichlet, source/sink terms, seepage faces, and atmospheric fluxes

Adaptive time stepping; Newton and Picard linearization; selection of CG-type linear solvers; etc









Overland (hillslope rills) and channel flow along s

DEM pre-analysis for definition of cell drainage directions, catchment drainage network and outlet, etc

"Constant critical support area": overland flow  $\forall$  cells with upstream drainage area  $A < A^*$ ; else channel flow (2 other threshold-based options also implemented)

Leopold & Maddock scaling relationships; Muskingum-Cunge solution scheme (explicit and sequential); etc

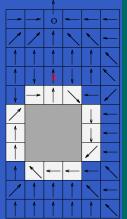
"Lake boundary-following" procedure to pre-treat lakes

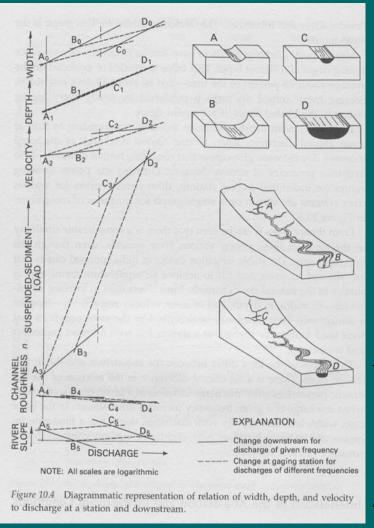
Storage and attenuation effects of lakes and other topographic depressions are accounted for by transferring with infinite celerity all the water drained by the "buffer" cells to the "reservoir" cell; level pool routing calculates the outflow from this cell:

 $\frac{\partial V}{\partial t} = I(t) - O(h^*)$ 



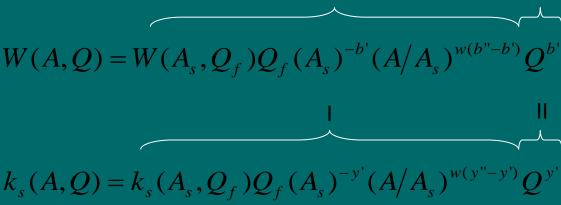
12	11	10	11	12	13
12	12	12	12	12	13
13	13	13	13	13	14
14	14	14	14	14	15
14	13	13	13	14	15
13	12	12	12	13	14
13	12	11	12	13	14
13	12	12	12	13	14
14	13	13	13	14	15
14	14	14	14	14	15
15	15	15	15	15	15





Surface runoff propagated through a network of rivulets and channels automatically extracted from the DEM.

Spatial (term I) and temporal (term II) variations of flow characteristics of the drainage network (stream channel geometry W and conductance coefficient  $k_s$ ) derived from application of downstream (according to upstream drainage area) and at-a-station (according to flow discharge) fluvial relationships:



\* From L. B. Leopold and T. Maddock Jr. (1953), "The hydraulic geometry of stream channels and some physiographic implications", U. S. Geological Survey, Professional Paper no. 252

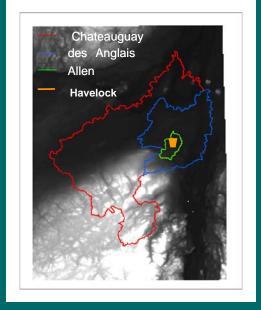
### Coupling, time stepping, and iteration

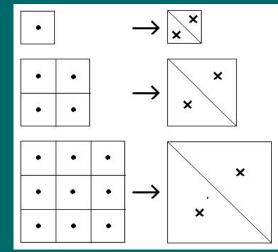
"Pond\_head\_min" threshold parameter accounts for microtopography

Coupled system solved sequentially<sup>\*</sup>: surface first, for  $Q^{k+1}$  and  $h^{k+1}$ ; then subsurface, for  $\psi^{k+1}$ ; finally overland flow rates  $q_L^{k+1}$  are back-calculated from subsurface solution [\*sequential solution procedure but with iterative BC switching during subsurface resolution to resolve the coupling]

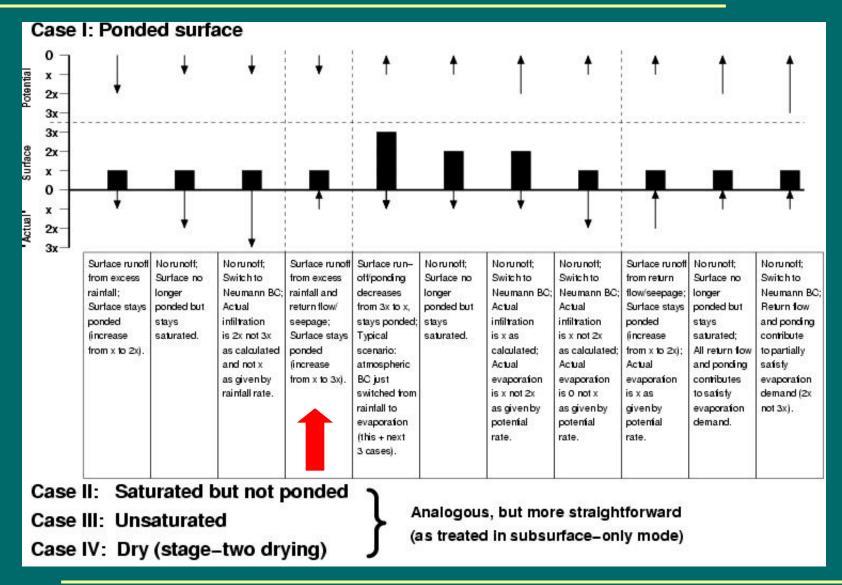
Nested time stepping: one or more surface solver time steps for each subsurface time step (based on Courant and Peclet criteria for the explicit surface routing scheme; also reflects typically faster surface dynamics compared to subsurface)

Interaction between cell-based surface grid and nodebased subsurface grid includes input option for coarsening of latter grid. Allows us to exploit slower subsurface dynamics and looser grid constraints (implicit scheme), and can lower CPU and storage costs of 3D module





#### Boundary condition-based coupling (surface BC switching procedure)



### Some recent studies (successes and challenges)

Recharge estimation, impact of heterogeneity

Hydrograph separation, model coupling approaches

**Bedrock leakage** 

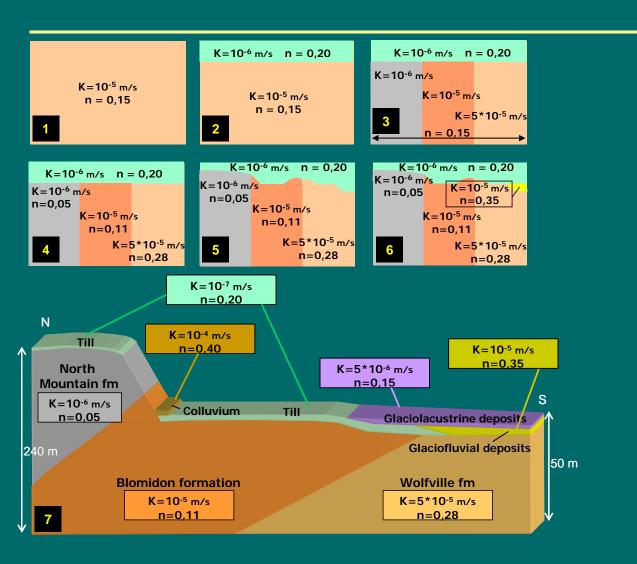
Predicting near-surface soil moisture state

Hysteresis in storage-discharge dynamics

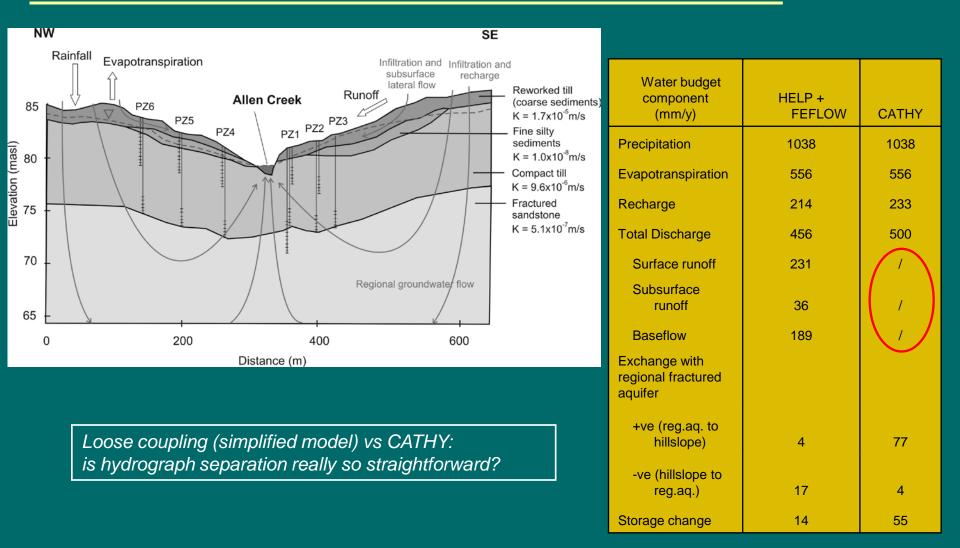
Rill flow vs sheet flow

Simulation of multiple response variables

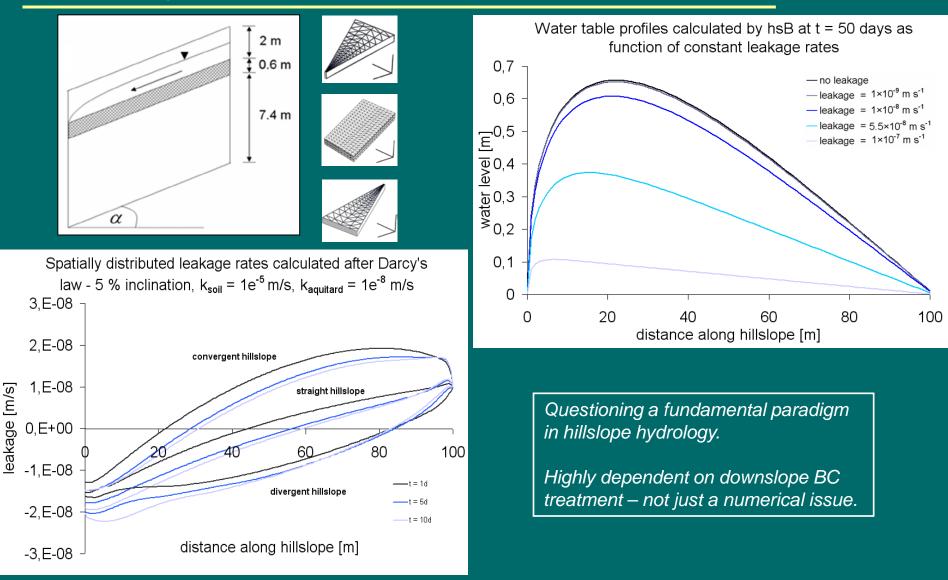
Problem of grid scale invariance



#### Hydrograph separation (Havelock hillslope, southwestern Quebec)

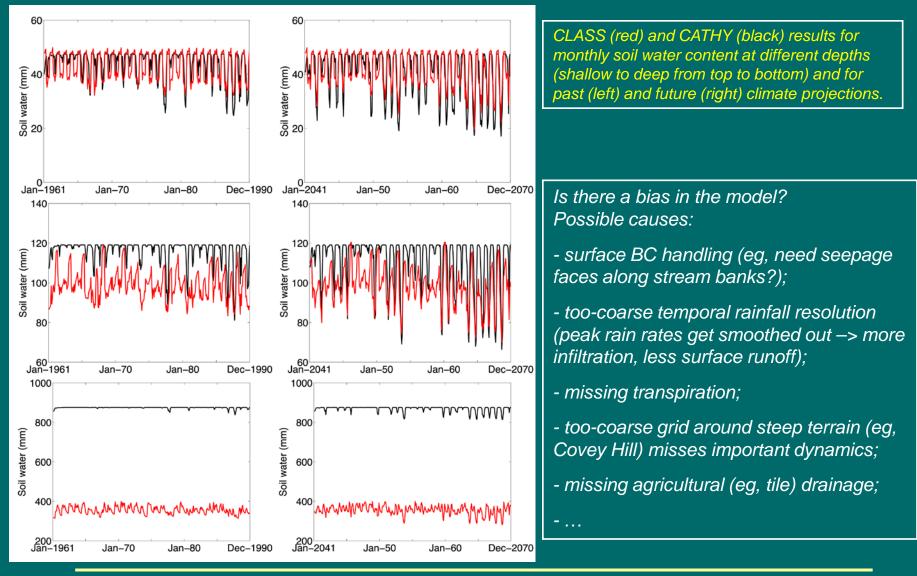


#### Bedrock leakage (idealized hillslopes / sloping unconfined aquifers)

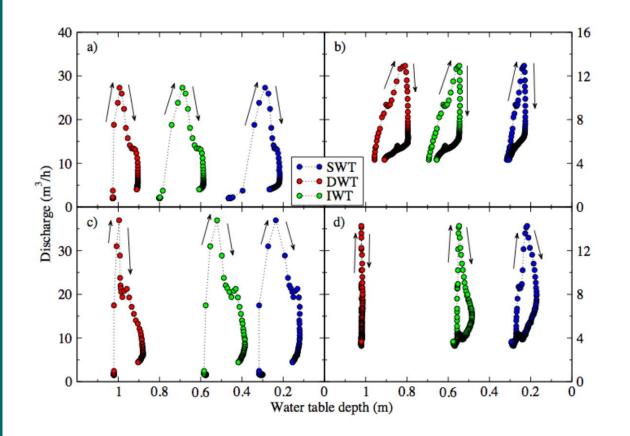


Broda, Paniconi, Larocque: J. Hydrol., 2011

#### Predicting near-surface soil moisture state (des Anglais river basin, southwestern Quebec)



Sulis, Paniconi, Rivard, Harvey, Chaumont: Water Resour. Res., 2011



CATHY can reproduce hysteresis and thresholding behavior observed in the relationship between the subsurface storage and discharge responses of a small catchment. No ad hoc parameterization is needed.

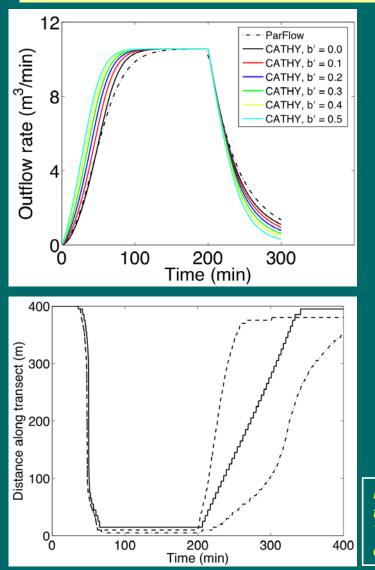
*Is there any link to or contribution from unsaturated zone hysteresis?* 

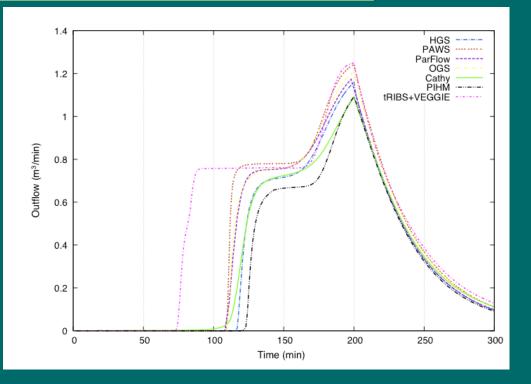
Nature and role of nonlinear phenomena in atmosphere– land surface–soil–aquifer interactions and feedbacks are poorly understood.

Simulated (top) and observed (bottom) responses in shallow, deep, and intermediate observation wells for 7-8 August 2009 (left) and 16-18 August 2009 (right) rainfall events.

Camporese, Penna, Borga, Paniconi: Water Resour. Res., 2014

#### Rill flow vs sheet flow (benchmark tests for model intercomparison)





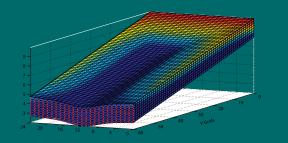
Benchmarking is a complicated business even for synthetic test cases ... Why and how do different models (even based on the same equations) perform differently? And what to do about it??

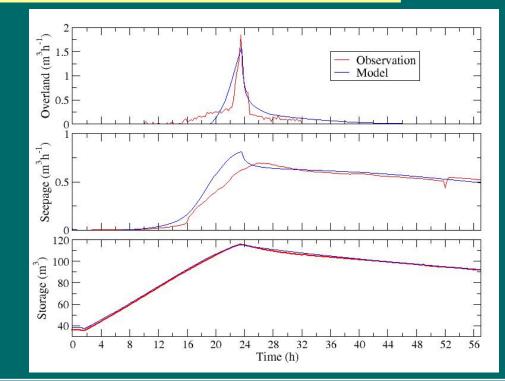
Evolution of the point of intersection between the water table and the land surface for the sloping plane test case. The outlet face is at x = 400 m. ParFlow: solid line; CATHY: dashed-dotted (sheet flow) and dashed (rill flow).

Sulis, Meyerhoff, Paniconi, Maxwell, Putti, Kollet: Adv. Water Resour., 2010 Maxwell, Putti, Meyerhoff, et al.: Water Resour. Res., 2014

#### Simulation of multiple response variables (Biosphere 2 Landscape Evolution Observatory)





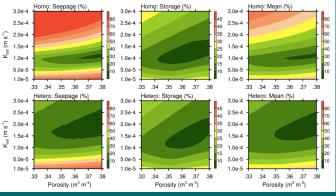


All three variables are integrated measures of the hillslope response. How does the model perform when we examine distributed responses? And what happens when we include solute transport?

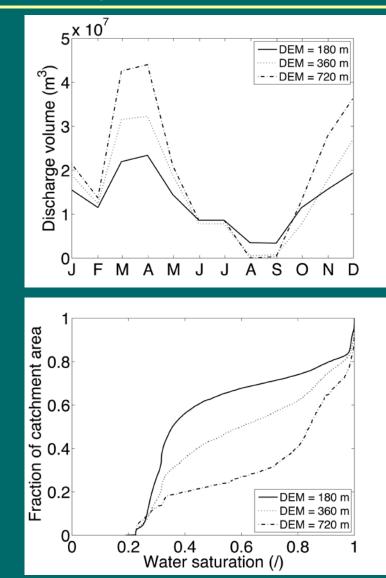
Issue of equifinality: does the mechanism we invoke imply (sole) causation?

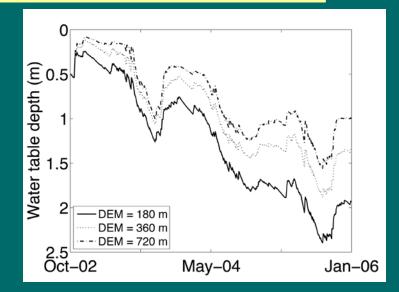
"Perfect knowledge" of the bottom BC ... how much does this help?

Niu, Pasetto, Scudeler, Paniconi, Putti, Troch: Hydrol. Earth Syst. Sci., 2014



#### Problem of grid scale invariance (des Anglais river basin, southwestern Quebec)





Comparison of simulation results at 3 different DEM resolutions: average monthly streamflow discharge, catchment-averaged daily water table depth, and cumulative frequency distribution of surface soil saturation after a 10-day rain period.

There are many reasons (causes) for grid scale invariance (and not limited to just the CATHY model). One of the most serious challenges in catchment-based hydrological / ecological modeling ...

Sulis, Paniconi, Camporese: Hydrol. Process., 2011

## Extensions and evolution of the model (flow and transport; other processes)

Flow (water quantity and distribution)

Surface

$$\frac{\partial \mathbf{Q}}{\partial t} + c_k \frac{\partial \mathbf{Q}}{\partial s} = D_h \frac{\partial^2 \mathbf{Q}}{\partial s^2} + c_k q_s$$

Subsurface

$$\sigma(\mathbf{S}_{w})\frac{\partial \psi}{\partial t} = \nabla \cdot \left[\mathbf{K}_{s}\mathbf{K}_{r}(\mathbf{S}_{w})(\nabla \psi + \eta_{z})\right] + \mathbf{q}_{s}$$

Transport (water quality and interactions with other substances)

 $\overline{}$ 

Surface

$$\frac{\partial \mathbf{Q}_m}{\partial t} + \mathbf{c}_t \frac{\partial \mathbf{Q}_m}{\partial \mathbf{s}} = D_c \frac{\partial^2 \mathbf{Q}_m}{\partial \mathbf{s}^2} + \mathbf{c}_t \mathbf{q}_{ts}$$

$$\frac{\partial \theta c}{\partial t} = \nabla \cdot \left[ -qc + D\nabla c \right] + q_{tss}$$

Weill, Mazzia, Putti, Paniconi: Adv. Water Resour., 2011

### Evolution of the model

Catchment/DEM-based

subsurface flow modeling 1993 saturated flow problems. Water Resour, Res., 30, 1994 Adv. Water Resour., 18, 1995 ariable density transport/ early coupled model) an el of coupled density-dependent flow and miscible salt transport. Seawater Intrusion in Coastal Aquifers, chap. 10, Kluwer Academic, 1999 Paniconi, Khlaifi, Lecca, Giacomelli, Tarhouni: Modeling and analysis of seawater intrusion in the coastal aquifer of eastern Cap-Bon, Tunisia. Transport in Porous Media, 43, 2001 Bixio, Gambolati, Paniconi, Putti, Shestopalov, Bublias, Bohuslavsky, Kastel Surface/Subsurface quation-based distributed hydrological model Adv. Water Resour., 26, 2003 low simulations in porous media. J. Comp. Phys., 208, 2005 ng in swelling/shrinking peat soils. **Vater Resour. Res.,** 42, 2006 approced was a series of the s Int, J. Numer, Meth, Fluids, 60, 2009 subsurface modeling with path-based routing, boundly condition-based coupling, and assimilation of multisource observation data. Water Resour. Res., 46, 2010 determination of number of the determination of the second second digital elevation models. Water Resour. Res., 39, 2003 assimilaanalVSISs-based catchment scale model of surface and subsurface flow. Water Resour. Res., 45, 2009 from gridded elevation data. Water Resour, R sics-based numerical modMs for simulating surface water–aroundwater interactions. Adv. Water Resour., 33, 2010 face hydrological model. Adv, Water Resour,, 34, 2011 assimilation 998 Surf/subsurf & flow/ transport Water Resour., 47, 2012 rCOUDING face water interactions. Hydrol. Process., 27, 2013 bsurface simulations and field observations. Adv, Water Resour., 59, 2013 Ecohydrological modeling (LSM coupling, Res., 50, 2014 vegetation, energy balance, CO<sub>2</sub>, nutrient cycles) diagnose integrated hydrology and feedbacks. Water Resour. R el using post-assimilation (EnKF) diagnostics of streamflow and in situ soil moisture observations. J. Hvdrol., 514, 2014 Detailed experiments, geophysical inversion, parameter estimation Landscapesensitivity & uncertainty analysis, model intercomparison,

biogeochemistry & soil weathering, sediment transport & erosion, soil freezing & snowmelt, preferential flow, unstructured grids, ...

# Collaborators

Paniconi. Putti: A comparison of Picard and Newton iteration in the numerical solution of multidimensional variably saturated flow problems. Water Resour, Res., 30, 1994 Orlandini, Rosso: Diffusion wave mode Mario it Pouttion Annamaria, Mazzian, Asce, 1, 1996 Putti, Cordes: Finite element approxim Matteo Camporese: Gabriele Manoli, Sara Bonetti – University of Padua, Italy Orlandini, Rosso: Parameterization of stream channel geometry in the distributed modeling of catchment dynamics, Water Resour, Res., 34, 1998 Gambolati, Putti, Paniconi; Three-dimensional model of coupled density-dependent flow and miscible salt transport. Seawater Intrusion in Coastal Aquifers, chap. 10, Kluwer Academic, 1999 Paniconi, Khlaifi, Lecca, Giacomelli, TaStefanosOrlandinicaGiovanni/Moretti/-OUniversityTof/Modena-and/Reggio Emilia, Italy Mazzla, Putt: High order Godunov mis Mauro Sulis rate now, at University of Bonn Germany vs., 208, 2005 Mazzia, Putti: Three dimensional Mixed Finite Element Finite Kolume approach for the solution of density dependent flow in porous media J. Comput. Appl. Math., 185, 2006 Putti, Sartoretto: Linear Galerkin vs mixed inhite element 2D flow fields. Int. J. Numer, Meth. Funds, 2009 Orlandini, Moretti, Franchini, Aldighieri Guo Patri based Mitthe determination of main special contractive drainage (SA) of the determination of main specia Camporese, Paniconi, Putti, Salandin: Ensemble Kalman filter data assimilation for a process-based catchment scale model of surface and subsurface flow. Water Resour, Res., 45, 2009 Orlandini, Moretti: Determination of su Cécilet Dagés a le INRA-Montpellier, France Sulis, Meverhoff, Paniconi, Maxwell, Putti, Kollet: A comparison of two physics-based numerical models for simulating surface water-groundwater interactions, Adv. Water Resour., 33, 2010 Sulis, Paniconi, Camporese: Impact of Damiano (Pasetto; Carlotta Scudelersund) INRS-Enderand Iniversity Of Carlotta Scudelersund) VRS-Enderand Orlandini, Tarolli, Moretti, Dalla Fontana: On the prediction of channel heads in a complex alpine terrain using gridded elevation data. Water Resour, Res., 47, 2011 Dages, Paniconi, Sulis: Analysis of coupling errors in a physically-based integrated surface water-groundwater model. Adv. Water Resour., 49, 2012 Pasetto, Camporese, Putti: Ensemble Kalman filter versus particle filter for a physically-based coupled surface-subsurface model. Adv, Water Resour., 47, 2012 Guay, Nastev, Paniconi, Sulis: Comparison of two modeling approaches for groundwater-surface water interactions. Hydrol, Process., 27, 2013 Weill, Altissimo, Cassiani, Deiana, Marani, Putti: Saturated area dynamics and streamflow generation from coupled surface-subsurface simulations and field observations. Adv, Water Resour., 59, 2013 Camporese, Penna, Borga, Paniconi: A field and modeling study of nonlinear storage-discharge dynamics for an Alpine headwater catchment. Water Resour, Res., 50, 2014 Manoli, Bonetti, Domec. Putti, Katul, Marani: Tree root systems competing for soil moisture in a 3D soil-plant model. Adv, Water Resour., 66, 2014 Camporese, Daly, Dresel, Webb: Simplified modeling of catchment-scale evapotranspiration via boundary condition switching. Adv. Water Resour., 69, 2014 from a modeling study of the first experiment at the Biosphere 2 Landscape Evolution Observatory, Hydrol, Earth Syst. Sci., in press, 2014